

--- 1 A heat engine absorbs 250 J of heat from a hot reservoir and rejects 110 J to a cold reservoir. What is the efficiency of this engine?

- A) 39.% B) 78.% C) 31.% D) 85.% E) 56.%

Solution:

The efficiency is  $(Q_h - Q_c)/Q_h = (250 - 110)/250 = 56\%$ .

The correct answer is: E

--- 2 A heat engine with an output of 300 W has an efficiency of 30% and works at a frequency of 10 cycles/second. How much heat is absorbed ( $Q_h$ ) and how much rejected ( $Q_c$ ) in each cycle?

- A)  $Q_h = 200. \text{ J}$   $Q_c = 140. \text{ J}$  B)  $Q_h = 143. \text{ J}$   $Q_c = 9.00 \text{ J}$  C)  $Q_h = 1000. \text{ J}$   $Q_c = 700. \text{ J}$   
 D)  $Q_h = 100. \text{ J}$   $Q_c = 70.0 \text{ J}$  E)  $Q_h = 129. \text{ J}$   $Q_c = 90.0 \text{ J}$

Solution:

The work done per cycle is the power divided by the frequency  $300 \text{ W}/10 \text{ Hz} = 30 \text{ J}$ . If the efficiency is  $\epsilon$ , the heat absorber per cycle is  $Q_h = W/\epsilon = 30 \text{ J}/0.300 = 100. \text{ J}$ . The heat rejected per cycle is  $Q_c = (1 - \epsilon)Q_h = 0.700 \times 100. \text{ J} = 70.0 \text{ J}$ .

The correct answer is: D

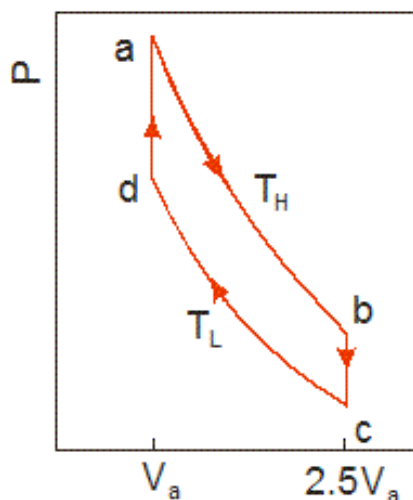


Figure 1: Problem 3

--- 3 Refer to Fig. 1. An ideal heat engine uses 0.300 mol of ideal gas and operates between a hot reservoir at  $T_H = 400 \text{ K}$  and cold reservoir at  $T_L = 300 \text{ K}$ , in a cycle from  $a \rightarrow b \rightarrow c \rightarrow d \rightarrow a$ . From  $a \rightarrow b$  the gas undergoes an isothermal expansion, changing its volume from  $V_a$  to  $2.5V_a$ . From  $b \rightarrow c$ , the pressure is reduced at a constant volume. From  $c \rightarrow d$ , the gas undergoes an isothermal compression, and from  $d \rightarrow a$ , the pressure is increased at a constant volume until the gas is back at the original condition at a. How much heat is absorbed in going from  $a \rightarrow b$ ?

- A) 1100. J B) 686. J C) 823. J D) 3050. J E) 914. J

Solution:

Process  $a \rightarrow b$  is isothermal. The internal energy of an ideal gas depends only on temperature so the heat in during an isothermal process is equal to the work done. That work is  $\int_{V_a}^{2.5V_a} P dV = nRT_H \ln(2.5V_a/V_a) = 914. \text{ J}$ .

The correct answer is: E

--- 4 Two refrigerators, one with a COP of 3.5 and another with a COP of 5.0, both extract 400 kJ of heat from the cold reservoir (food). Calculate the difference in energy they exhaust to the hot reservoir and hence the room.

- A) 34. kJ B) 24. kJ C) 38. kJ D) 31. kJ E) 41. kJ

Solution:

The difference is  $Q_c(1/COP_1 - 1/COP_2) = 400(1/3.5 - 1/5.0) \text{ kJ} = 34. \text{ kJ}$ .

The correct answer is: A

--- 5 A water-cooled electric power plant generates 250 MW of power at an efficiency of 35.0%. At what rate must water be circulated past the condenser if the change in water temperature is not to exceed 10 °C? (The specific heat of water is  $4.2 \times 10^3 \text{ J/kg } ^\circ\text{C}$ )

- A) 11100. kg/s B) 8840. kg/s C) 2630. kg/s D) 6630. kg/s E) 111000. kg/s

Solution:

The power produced is 250 MW. The power consumed by the plant is  $P/0.350 = 714. \text{ MW}$  The heat energy per unit time rejected by the plant into the environment is  $P_Q = P - P/0.350 = 464. \text{ MW}$ . If the cooling water undergoes a temperature increase of  $\Delta T$ , and if water has a specific heat of  $c$ , the mass of water consumed per unit time is  $P_Q/c\Delta T = 11100. \text{ kg/s}$ .

The correct answer is: A

--- 6 What is the maximum possible coefficient of performance of a heat pump that is capable of maintaining the interior of a house at 28 °C when the temperature outside is -40 °C?

- A) 0.44 B) 0.41 C) 4.4 D) 0.56 E) 3.4

The maximum COP is  $T_h/(T_h - T_c) = 301/(301 - 233) = 4.4$ .

The correct answer is: C

1. E

2. D

3. E

4. A

5. A

6. C